

MATRICES AND UNITS IN QUATERNION ALGEBRAS  
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In this talk we will study the group of units  $R^*$  of an order  $R$  in a non-split quaternion algebra  $\left(\frac{-1,-1}{K}\right)$  with coefficients in a number field  $K$ . First we will explain how to study this group, in general, through the action of its elements both on the three dimensional hyperbolic space  $H^3$  and on the quadratic module

$$(K^3, q) = \begin{cases} K^3 = Ki \oplus Kj \oplus Kk, \\ q(ai + bj + ck) = a^2 + b^2 + c^2. \end{cases}$$

Next we will look at the case of imaginary quadratic fields, concentrating on the case  $K = \mathbb{Q}(\sqrt{-7})$ . This topic has also potential interest for wireless multiantenna communications in terms of space-time code construction.