Computational Methods in Inverse Problems, Mat-1.3626

Fall 2007

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MATLAB PRIMER – HOW TO GET STARTED

Matlab is a high level programming language particularly suitable for numerical linear algebra. The basic object in Matlab are matrices and vectors. To create arrays

$$x = \begin{bmatrix} 2\\ -3\\ 1 \end{bmatrix}, \quad A = \begin{bmatrix} 1 & 0 & 4\\ -1 & 2 & 1\\ -2 & 6 & 0 \end{bmatrix},$$

the comands are

x = [2;-3;1]; A = [1,0,4;-1,2,1;-2,6,0];

If you leave the semicolon at the end of the line out, Matlab echoes the array, which may be a good way to check that you did not do errors.

Matrix products and transposes: To calculate

$$y = Ax, \quad B = A^{\mathrm{T}},$$

type

To extract rows and columns from a matrix: Given the matrix A above, if you want the first column of A, or a submatrix containing only the first two rows of A, that is

$$\begin{bmatrix} 1\\ -1\\ -2 \end{bmatrix}, \begin{bmatrix} 1 & 0 & 4\\ -1 & 2 & 1 \end{bmatrix},$$

you may type simply

A(:,1) A(1:2,:)

More generally, if C is a $n \times m$ matrix and you want to create a submatrix containing only j rows whose numbers you have collected to an index vector $I = [k_1, k_2, \ldots, k_j]$, write

C(I,:)

Conversely, if you want to merge two column vectors of same length into an array, try this:

a = [4;0;-1]; b = [1;2;0]; A = [a,b];

The result is a 3×2 array *a* and *b* as its columns.

Plot command in Matlab are versatile and of great help, e.g., when debugging a code. Suppose you want to plot the function $t \mapsto t \cos(\pi t)$, $0 \le t \le 1$. What you have to do is to form a vector discretizing the interval by n sampling points and another vector containing the function evaluations at those points:

n = 100; t = linspace(0,1,n); y = t.*cos(pi*t); plot(t,y)

Notice the difference between the matrix product "*" and the pointwise multiplication of two vectors of equal size, "*.".

Solving linear systems: Let A be a square matrix of size $n \times n$ and b a column vector of size n. To find the n-vector x satisfying

Ax = b,

the Matlab command is

 $x = A \ ;$

If the matrix is not invertible or very ill-conditioned, Matlab lets you know (Try!). If you have a non-square matrix $A \in \mathbb{R}^{m \times n}$ and a column vector $b \in \mathbb{R}^m$, the command above returns the Least Squares Minimum Norm (LSQMN) solution, which can be written in terms of the pseudo-inverse of A,

$$x = A^{\dagger} b \in \mathbb{R}^n$$

The Singular Value Decomposition (SVD) of a matrix,

 $A = UDV^{\mathrm{T}},$

is obtained by the command line

[U,D,V] = svd(A);

Suppose you want to plot the singular values in a logarithmic scale. You may try the commands

d = diag(D);
plot(log(d));

giving you a curve plot. If you want to plot the singular values as red dots, you may try

plot(log(d),'r.','MarkerSize',15)

An automatic scaling to logarithmic scale, with slightly smaller blue dots, you get by typing

semilogy(d,'b.','MarkerSize',10)

More Matlab appears on these pages as the course goes on.