Visa Latvala, Niko Marola, Mikko Pere: *Harnack's inequality for a nonlinear eigenvalue problem on metric spaces*; Helsinki University of Technology, Institute of Mathematics, Research Reports A484 (2005).

**Abstract:** We prove Harnack's inequality for first eigenfunctions of the p-Laplacian in metric measure spaces. The proof is based on the famous Moser iteration method, which has the advantage that it only requires the (1, p)-Poincaré inequality. As a by-product we obtain the continuity and the fact that first eigenfunctions do not change sign in bounded domains.

## AMS subject classifications: 35P30, 35J20

Keywords: Sobolev space, Newtonian space, Caccioppoli estimate, Harnack's inequality, First eigenvalue, First eigenfunction, Rayleigh quotient, p-Dirichlet integral, Moser iteration

## Correspondence

Visa Latvala Department of Mathematics, University of Joensuu, P.O. Box 111 FI-80101 Joensuu, Finland; visa.latvala@joensuu.fi

Niko Marola Institute of Mathematics, Helsinki University of Technology, P.O. Box 1100 FI-02015 Helsinki University of Technology, Finland; nmarola@math.hut.fi

Mikko Pere Department of Mathematics and Statistics, University of Helsinki, P.O. Box 68 FI-00014 University of Helsinki, Finland; mikko.pere@helsinki.fi

ISBN 951-22-7599-6 ISSN 0784-3143

Helsinki University of Technology Department of Engineering Physics and Mathematics Institute of Mathematics P.O. Box 1100, 02015 HUT, Finland email:math@hut.fi http://www.math.hut.fi/