

mplD002R.mw

a)

```
> y:=C*exp(-x)+x^2-2*x; # RE
```

$$y := C e^{-x} + x^2 - 2x \quad (1.1.1)$$

```
> vasen:=diff(y,x)+y;
```

$$\text{vasen} := -2 + x^2 \quad (1.1.2)$$

```
> oikea:=x^2-2;
```

$$\text{oikea} := -2 + x^2 \quad (1.1.3)$$

```
> vasen=oikea;
```

$$-2 + x^2 = -2 + x^2 \quad (1.1.4)$$

Tarkistus oli helppoa. Miten sitten löytäisimme RE:n Katotaan, osaako Maple.

Maplessa on dsolve-komento diffyhtaloihin. Kokeillaan, osaako se..

```
> y:='y':x:='x':
```

```
> dy:=diff(y(x),x)+y(x)=x^2-2; # Diffyht%l^n esitysmuoto
```

$$dy := \frac{d}{dx} y(x) + y(x) = -2 + x^2 \quad (1.1.5)$$

```
> dsolve(dy,y(x));
```

$$y(x) = -2x + x^2 + e^{-x} _C1 \quad (1.1.6)$$

b)

```
> y:=a*cos(x)+b*sin(x);
```

$$y := a \cos(x) + b \sin(x) \quad (1.2.1)$$

```
> diff(y,x,x)+y;
```

$$0 \quad (1.2.2)$$

Kyl vaan! Kokeillaan taas dsolvea:

```
> y:='y':
```

```
> dsolve(diff(y(x),x,x)+y(x)=0,y(x));
```

$$y(x) = _C1 \sin(x) + _C2 \cos(x) \quad (1.2.3)$$

Joooo!

c)

```
> d3y:=exp(x);
```

$$d3y := e^x \quad (1.3.1)$$

```
> d2y:=int(dy3,x)+c1;
```

$$d2y := dy3 x + c1 \quad (1.3.2)$$

```
> d1y:=int(dy2,x)+c2;
```

$$(1.3.3)$$

$$dly := dy2 x + c2 \quad (1.3.3)$$

```
> y:=int(dy1,x)+c3;
```

$$y := dy1 x + c3 \quad (1.3.4)$$

Tarkistus:

```
> diff(y,x,x,x);
```

$$0 \quad (1.3.5)$$

```
> y:='y': dsolve(diff(y(x),x,x,x)=exp(x),y(x));
```

$$y(x) = e^x + \frac{1}{2} _C1 x^2 + _C2 x + _C3 \quad (1.3.6)$$

d)

```
> restart;
```

```
> REh:=x^2+y(x)^2=C;
```

$$REh := x^2 + y(x)^2 = C \quad (1.4.1)$$

```
> diff(REh,x);
```

$$2x + 2y(x) \left(\frac{d}{dx} y(x) \right) = 0 \quad (1.4.2)$$

```
> dsolve(%,y(x),implicit);
```

$$y(x)^2 + x^2 - _C1 = 0 \quad (1.4.3)$$

```
> dsolve(%%,y(x));
```

$$y(x) = \sqrt{-x^2 + _C1}, y(x) = -\sqrt{-x^2 + _C1} \quad (1.4.4)$$